Using the Imperialistic Competitive Algorithm Model in Bankruptcy Prediction and Comparison with Genetic Algorithm Model in Listed Companies of Tehran Stock Exchange

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ABSTRACT
Bankruptcy prediction is a major issue in classification of companies. Since bankruptcy is extremely costly, investors, owners, managers, creditors, and government agencies are interested in evaluating the financial status of companies. This study tried to predict bankruptcy among companies registered in Tehran Stock Exchange (Iran) by designing imperialist competitive algorithm and genetic algorithm models. It then compared the accuracy of the two models in financial conditions of Iran and sought the best model to predict company bankruptcy one, two, and three years before its incidence. Also uses a model to surveying the financial position and also the subject of continuing operations about them to improve the quality of decision taken by shareholders and stakeholders. The study sample consisted of 38 bankrupt and 38 non-bankrupts companies during 2007-2016. The final variables used in both algorithms were five financial ratios. The results showed that the imperialist competitive algorithm had better accuracy than the genetic algorithm in bankruptcy prediction at the mentioned intervals.

Keywords:
Bankruptcy prediction, financial ratios, genetic algorithm, imperialist competitive algorithm, Tehran Stock Exchange.
1. Introduction

In recent decades, globalization, emergence of new markets, higher competition between companies, institutions, and organizations, and rapid economic, social, and technological changes have increased uncertainty and volatility in financial environment and complicated the financial decision-making process. In such conditions, untimely and inefficient investments will cause significant macroeconomic challenges for a country, i.e. economic development will widely depend on appropriate decision-making and effective resource allocation. The absolute support provided by all developed and developing economies for investments and investors has turned investments and taking advantage of investment opportunities into a critical issue in financial management. Decision-making (choosing one way among different solutions) is an indispensable part of management. On the other hand, making any decision requires the acquisition, processing, analysis, and appropriate inference from available data. Therefore, models to predict financial status of a corporate will be of great help to investors who are often forced to make quick decisions about their investments while they may lack an analytical understanding of corporates (Aziz & et al, 2006).

Financial distress and the consequent bankruptcy experienced by numerous companies in different countries has forced capital market participants and researchers to strive for ways to predict such situations and protect the investors’ investments. Several Iranian companies, even those registered in Tehran Stock Market, are suffering from financial distress, e.g. some companies are facing difficulty in repaying their debts, some lack enough incoming cash flow to pay their operating costs, and some are subject to article 141 of the Iranian commercial law.

These corporates have in fact wasted their resources instead of investing them in profitable opportunities and value-added economic activities and are hence at risk of bankruptcy or liquidation. Consequently, they can be easily identified through assessments of financial statements and reports provided by statutory auditors. As corporate bankruptcy or liquidation will generally affect different groups of stakeholders (e.g. shareholders, managers, employees, and creditors), great efforts have been made by researchers and capital market participants to design and develop models to predict corporate financial distress. Such models aim to identify indices facilitating the prediction of a company’s future status and can be useful in making appropriate investments and prohibiting waste of resources.

Faster detection of financial distress indicators can warn companies about the possibility of financial distress and pressurize them to take necessary preventive measures. It can also help investors discriminate between favorable and poor investment opportunities and stay away from the latter (Permacahndra, 2009). Bankruptcy prediction and intrusion detection models are techniques and tools which can predict the future status of the companies and estimate the probability of financial distress through combining a group of financial ratios. These models can be classified into three groups Statistical (multiple discriminant analysis models, linear probability, logit, probit, cumulative totals, and partial adjustment process), Artificial intelligence (artificial neural networks, recursive neural networks, genetic algorithms, support vector machines, rough sets, induction, deduction, and fuzzy logic) and theoretical models (balance sheet analysis/entropy, bankruptcy speculator theory, cash management theory, and credit risk theory). Statistics-based and artificial intelligence approaches focus on signs and symptoms of bankruptcy, while theoretical models solely concentrate on reasons and causes of bankruptcy (Aziz & et al, 2006). Data mining techniques have been applied as a new approach for intrusion detection. Bankruptcy prediction is one of the most special economic grounds of data mining which have been much investigated in recent years. In order to compare the accuracy of imperialist competitive algorithm and genetic algorithm in corporate bankruptcy prediction, the current research presents the literature review, introduces the genetic algorithm and the proposed algorithm, develops hypotheses, describes the research design, and finally makes conclusions.

2. Literature Review

Considering the importance of financial distress and bankruptcy prediction, numerous studies in this field have been conducted in Iran and other countries. The earliest studies (1935) in the case of bankruptcy prediction were performed by A.H. Winakor and R.F Smith who found financial ratios to be appropriate predictors of financial problems. Through the next
research in 1942, Charles Merwin introduced a model with three variables of working capital to total assets ratio, equity to total debt ratio, and current ratio. In 1996, William Beaver used univariate analysis and could successfully predict financial stress five years before its occurrence in 78% of cases.

Later studies evaluated multivariate models. For instance, Edward Altman selected 22 financial ratios and analyzed them by using z-scores of five ratios. The accuracy of his model was about 95% and 83% in predicting bankruptcy one and two years prior to the event, respectively (Altman E.L., 1968). In 1993, Altman used four financial ratios instead of five to increase the predictive power of his model for non-manufacturing companies and provided more accurate prediction. Ohleson (1980) developed a model by applying the logit function on nine financial ratios as independent variables. Five of these ratios had been used in previous studies. Based on comparisons between 46 bankrupt companies and a number of successful companies during 1969-76, Taffell presented a model to predict bankruptcy (Taffell J., 1984). King Don et al. (1995) were the first to use a genetic algorithm in bankruptcy prediction. Studying a sample of 236 bankrupt and 264 non-bankrupt companies through genetic algorithm, Varetto et al. (1998) reported an accuracy of 93.0% and 91.6% in predicting bankruptcy one and two years before the event, respectively. McKee et al. (2000) criticized previous studies in the field of bankruptcy prediction and used the recursive partitioning algorithm (decision tree) with six ratios as independent variables for this purpose. Shah and Murtaza (2002) predicted bankruptcy with a model based on an artificial neural network. After assessing data from 60 bankrupt and 54 non-bankrupt firms between 1992 and 1994, they calculated the accuracy of their model as 73%. Shin and Lee (2002) suggested genetic models as suitable, easy to use models to predict financial distress.

Kawakami et al (2004) compared the pre-selection algorithm, genetic algorithm, and multi-discriminant analysis and introduced the first and last methods as the most and least favorable, respectively. Min and Lee (2005) concluded that support vector machines had better performance in bankruptcy prediction than traditional statistical models. Lensberg et al (2006) used genetic programming for 28 potential bankruptcy variables previously identified as significant and found six variables to be important. Min et al. (2006) applied the genetic algorithm and a support vector machine simultaneously and called it the GA-SVM model. Wu et al. (2007) developed a support vector machine model based on the genetic algorithm to obtain optimized parameters. They reported the model to have important advantages (better prediction accuracy and generalizability) over other methods. Alforo et al. (2008) applied two AdaBoost algorithm and artificial neural networks models to predict financial distress. Their findings showed that AdaBoost algorithm performs %91 better than artificial neural networks. Ahn and Kim (2009) found that combining case-based reasoning (CBR) and genetic algorithms can significantly increase the accuracy of prediction.

Premachandra et al. (2009) proposed data envelopment analysis (DEA) as a quick-and-easy tool for assessing corporate bankruptcy. DEA is a non-parametric method that measures weight estimates (not parameter estimates) of a classification function for separating default and non-default firms. They used nine financial variables (two outputs and seven inputs) that proxy for the financial strength/weakness and potential insolvency of firms. Estimation accuracy for out-of-sample firms is about %86, while for others equals %89. Li and Sun (2009) examined financial distress prediction (FDP) using support vector machines (USM) (ensemble vs. individual). They proposed a new FDP method based on SVM ensemble, whose candidate single classifiers are trained by SVM algorithms with different kernel functions on different feature subsets of one initial dataset. Their achieved findings indicated that during a year before financial distress, neural networks perform better than logistic regression approaches, while in consecutive two years, logistic regression approach with %85.32 prediction can perform better than neural networks with %83.33 prediction. Gepp et al. (2010) applied decision trees approach for intrusion detection and concluded that this approach is appropriate for detection. Xie and et al (2011) sought to predict financial distress in Chinese manufacturing firms by support vector machines and multi-discriminant analysis and found the first to have better predictive power. Cheng (2012) proposed a new approach through combining the traditional bankruptcy model and Altman’s model according to characteristics of the board of directors. Findings of this study showed that Altman’s model is valid and accurate. It can be also concluded that the new proposed approach improves prediction process.
Mousavi Shiri et al. (2012) studied DEA on a sample of 60 companies listed on Tehran Stock Exchange over a period from 2000 to 2010 and examined the efficiency of financial distress prediction. Findings of this study indicated that efficiency plays a significant role in financial distress prediction so that it demonstrates necessary signs for bankruptcy from two years before. Moradi et al. (2013) applied FCM and support vector data description (SVDD) to the financial distress prediction problem in an attempt to suggest a new model with better explanatory power and stability. To evaluate the prediction accuracy of SVDD, they compared its performance with fuzzy c-means (FCM). According to the data obtained from 24 financial ratios between 2000 and 2009, 70 pairs of companies listed on Tehran Stock Exchange were selected as initial data set. Results from algorithm test based on support vector data description show that model accuracy in classifying financial distress samples in the financial distress occurrence year, One and two years before it, is 91.9%, 85% and 78% respectively. While results from algorithm test based fuzzy c-means indicated that model accuracy in classifying financial distress samples in the financial distress occurrence year, One and two years before it, is %96.67, %83.44 and %77.34 respectively. Rostami et al. (2013) compared Support Vector Machine and Particle Swarm Optimization algorithm models and investigated a sample of 79 healthy and 79 bankrupt companies from 2005 to 2010. Based on related and previous articles 56 financial ratios on classifying profitability, liquidity, operating and financial leverage were chosen as the independent variables. The results indicate that the Support Vector Machine algorithm had better ability for predicting bankruptcy in comparison with particle swarm optimization algorithm. Kim et al. (2014) used decision tree and AdaBoost-decision tree algorithms in order to predict financial distress for a sample of 722 restaurants from 1988 to 2010. Their findings proved the superiority of AdaBoost-decision tree algorithm and its lower error. In addition, the most significant ratio in this study was liability to shareholders’ equity. Golet (2014) examined binary regression to predict bankruptcy. He conducted this study in Romania from 2008 to 2012 and found that fixed assets ratio, fixed assets turnover, working capital and ownership ratio have negative effect on bankruptcy risk, while collection period has a positive effect.

Bredart (2014) applied artificial neural networks and three variables of shareholders’ equity (property from financial status classification, current ratio from equity classification, the ratio of net income to property from profitability classification) studied bankruptcy prediction in Belgium from 2002 to 2012. His findings indicated %80 success of neural network in bankruptcy prediction. In this study, a model of imperialistic competitive algorithm which considered as one of the first time bankruptcy prediction models in Iran and also considered as one of the artificial intelligence models that have been studied and finally, the results of this model are compared with the genetic algorithm. Gang et al. (2015) in a research attempt to predict the financial distress of 107 Chinese companies listed on the stock market between 2001 and 2008 using data mining techniques. Accordingly, using this technique, financial distress alert models were designed and built. The results of the research with a comparative approach showed that neural networks have more predictive accuracy than Support Vector Machine and decision tree. Salehi et al. (2016) used a sample of 159 companies during the years 2011-2014 on Tehran Stock Exchange to predict the financial distress using data mining techniques. Their research results show that the Artificial Neural Networks (ANN) better serves the k-Nearest Neighbor (KNN) and Naïve Bayesian Classifier (NBC) bankruptcy prediction. Wagle et al. (2017) in their research, used neural network data mining techniques, backup machines, Bayesian networks and logistic regression, and 120 companies with 30 financial ratios to predict corporate bankruptcy. Their research results showed that the artificial neural network has better predictive power than other models.

3. Methodology

3.1 Overview of Imperialist Competitive Algorithm

The novel Imperialist Competitive Algorithm (ICA) that was introduced in 2007 has a good performance in some optimization problems. The ICA inspired by socio-political process of imperialistic competition of human being in the real world. This algorithm starts by generating a set of candidate random solutions in the search space of the optimization problem. The generated random points are called the initial Countries. Based on their power,
some of the best initial countries (the countries with the least cost function value), become Imperialists and start taking control of other countries (called colonies) and form the initial Empires. The absorption policy makes the main core of this algorithm and causes the countries move towards to their minimum optima. The imperialists absorb these colonies towards themselves with respect to their power. The total power of each imperialist is determined by the power of its both parts, the empire power plus percents of its average colonies power.

\[ T.C.n = \text{Cost (imperialist)} + \xi \text{ mean } \{\text{Cost (colonies of empire}_n)\} \] (1)

Imperialist competitive algorithm process can be summarized as follows:

1. Select some random points on the function and initialize the empires.
2. Move the colonies toward their relevant imperialist (assimilation).

Fig.2 shows the movement of a colony towards the imperialist. In this movement, \( \theta \) and \( x \) are random numbers with uniform distribution as illustrated in formula (2) and \( d \) is the distance between colony and the imperialist.

\[ x \sim U(0, \beta \times d), \theta \sim U(-\gamma, \gamma) \] (2)

Where \( \beta \) and \( \gamma \) are parameters that modify the area that colonies randomly search around the imperialist. In our implementation \( \beta \) and \( \gamma \) are considered as 2 and 0.5 (Radian) respectively.

3. During assimilation and revolution a colony might reach a better position and has the chance to take the control of the entire empire and replace the current imperialist state of the empire.

\[ \text{Figure 1. Initial imperialist formation} \]

\[ \text{Figure 2. Moving colonies toward their imperialist (Assimilation process)} \]
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3. Replacement of imperialist and colony

Figure 4. Total empire (after replacement)

4. Compute the total cost of all empires (considering the cost of both imperialist and its colonies).
5. Pick the weakest colony (colonies) from the weakest empire and give it (them) to the empire that has the most likelihood to possess it (Imperialistic competition).

6. Eliminate the powerless empires.
7. If there is just one empire, then stop else continue and go to stage 2. Algorithm continues with the mentioned steps until a stop condition is satisfied and there is only one empire (Atashpaz-Gargari and et al.2007).

3.2. Introduction to Genetic Algorithms

Fundamental principles of the genetic algorithm were introduced by John Holland (from the University of Michigan) in 1975. Later in 1989, Goldberg developed the concepts of the genetic algorithm (Goldberg, D.E, 1989). Genetic algorithm is a probabilistic search method which mimics natural evolution. This algorithm utilizes the survival of the fittest to produce better estimates of the response from a population of potential solutions. In each generation, a set of solutions is created through selecting individuals with the highest fitness in the problem domain and breeding those using genetic operators. This process evolves the first population toward a new one with better fitness compared to its parents. The overall structure of the genetic algorithm is as follows:

1) Genes and chromosomes: Genes, the smallest building blocks of the genetic algorithm, are used to encode the parameters. Each string of genes (called a chromosome) is a proposed solution to the problem which may or may not be appropriate (Sinriech, D, Samakh, E, 1999).
2) Population: A set of chromosomes is called a population. A main characteristic of the genetic algorithm is focusing on a population of chromosomes rather than one point of the solution domain (Fogarty, T.C, 1989).
3) Fitness function: It determines how well individuals can solve the problem. In this study, the fittest individuals had the value of the fitness function (Van larhoven, P.J.M, Aarts. E.H.L, 1987).
4) Genetic operators: A new generation of solutions (children) can be obtained by applying genetic operators on the previous generation. Genetic operators include:
   a) Crossover: It combines two randomly selected chromosomes (parents) to produce two new chromosomes (children). A significant concept associated with this operator is the crossover rate which is obtained by dividing the number of created children in each generation to the population size (Van larhoven, P.J.M, Aarts. E.H.L, 1987).
   b) Mutation: In natural evolution, mutation is a random process through which the content of a gene is replaced with that of another
gene to produce a new genetic structure. In the genetic algorithm, mutation reassures that all strings will be searched (the probability of search will not be zero in any string) (Van larhoven, P.J.M., Aarts, E.H.L., 1987).

c) Generation: Each iteration of the algorithm that leads to creation of a new population is called a generation (Powell, D and Skolnick, M, 1993).

Iterations continue until a pre-defined termination condition, e.g. obtaining the maximum number of generations or an acceptable level of competence, is reached.

3.3. Research Hypotheses
Based on the research objectives, the following hypotheses were considered:

3.3.1. The First Group of Hypotheses
The first two hypotheses related to the capability of the models in predicting corporate financial distress prediction:

1) The first hypothesis: Financial distress of companies registered in Tehran stock market can be predicted with imperialist competitive algorithm.

2) The second hypothesis: Financial distress of companies registered in Tehran stock market can be predicted with genetic algorithm.

3.3.2. The Second Group of Hypotheses
The third hypothesis tried to find probable significant differences between the two models in the current financial environment of Iran environmental conditions.

3) Third hypothesis: The overall accuracy of the predictions made by imperialist competitive algorithm and genetic algorithm is different.

3.3.3. The Research Sample
Companies registered in Tehran stock market constituted the research population. Therefore, two statistical samples were included in this study, i.e. 38 companies experiencing financial distress (according to the article 141 of the Iranian commercial law) and 38 successful companies were selected from their relevant populations. Also in this study, used paired samples.

3.4. Sampling
3.4.1. Selecting Distressed Companies
A list of companies subject to the article 141 of the Iranian commercial law during 2010-16 was prepared. Due to the inaccessibility of data, this seven-year period was considered as the research time span. Since the models designed in this study were tested one, two, and three years prior to the incidence of financial distress, the analyzed data actually belonged to 2007-16. Although the initial list included 452 companies, the financial data of only 140 companies was fully accessible. After selecting 70 companies as the sample, 38 companies were finally recruited to increase accuracy. All models in this study have been implemented through the application of Toolbox NNTool coding in Matlab Software (2011).

3.4.2 Selecting Successful Companies
As mentioned, paired samples were used in this study. Hence, a uniquely matched successful company was selected for each previously selected distressed company. Successful companies were only included if they matched their distressed counterparts in terms of financial data availability during a three-year period and size or industry. A successful company with the closest total assets to that of a distressed company at the time of financial distress (year 1) and accessible financial data during the three earlier years (year’s t-1, t-2, and t-3) was selected as the counterpart of the distressed company. For bankrupt companies, the based year (t) is the year when the company becomes subject to the article 141 of Iranian commercial law. For successful companies, however, it is defined as the year when the company gains the highest retained earnings.

Unfortunately, we failed to match the companies in terms of industry due to the low number of successful and distressed companies in one industry or a group of similar industries. Therefore, we sought to match the samples based on size (according to the logarithm of total assets). Considering that the companies’ logarithm of total assets differed in range, the mentioned process could have enhanced the generalizability of the designed models. Finally, 38
successful companies matching distressed samples in the range of logarithm of total assets were selected.

3.5. Research Variables

Determining and defining variables is dispensable to every research. This study included independent and dependent variables.

3.5.1. Independent Variables

Financial ratios constituted independent variables in the analysis of the genetic algorithm model section.

3.5.2. Dependent Variables

Belonging a company to either distressed or successful groups was considered as the dependent variable in all the developed models in this study.

Table 1: Financial Ratios

<table>
<thead>
<tr>
<th>Financial ratios</th>
<th>Calculation method</th>
<th>Financial ratios</th>
<th>Calculation method</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cash flow ratios</td>
<td></td>
<td>Profitability ratios</td>
<td></td>
</tr>
<tr>
<td>X1_1</td>
<td>operating cash flow / total liabilities</td>
<td>X12</td>
<td>Earnings before interest and taxes / total assets</td>
</tr>
<tr>
<td>X1_2</td>
<td>operating cash flow / current liabilities</td>
<td>X13</td>
<td>Retained earnings / total assets</td>
</tr>
<tr>
<td>X1_3</td>
<td>operating cash flow / current assets</td>
<td>X14</td>
<td>Interest expenses / liability - dividends payable</td>
</tr>
<tr>
<td>X1_4</td>
<td>operating cash flow / working capital</td>
<td>X15</td>
<td>Interest expenses / sales</td>
</tr>
<tr>
<td>Liquidity ratios</td>
<td></td>
<td>Leverage ratios</td>
<td></td>
</tr>
<tr>
<td>X6_6</td>
<td>quick ratio</td>
<td>X16</td>
<td>total debt / total assets</td>
</tr>
<tr>
<td>X1_7</td>
<td>working capital / total asset</td>
<td>X17</td>
<td>Earnings before interest and taxes / interest expenses</td>
</tr>
<tr>
<td>Activity ratios</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X1_8</td>
<td>net sales / total asset</td>
<td>X18</td>
<td>net profit / sales</td>
</tr>
<tr>
<td>X1_9</td>
<td>inventory turnover</td>
<td>X19</td>
<td>return on investment</td>
</tr>
<tr>
<td>X1_10</td>
<td>net sales / working capital</td>
<td>X20</td>
<td>interest expenses / working capital</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
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</tbody>
</table>
|                        | In the third stage, five variables (X1_1, X1_2, X1_5, X1_7, and X1_9) were selected using the genetic algorithm. A company is bankrupt only if X1_1 < 0.082, X1_2 < 5.43, X1_7 < 1.146, X1_10 > 0.726, and X1_9 < -0.62. Otherwise, it is non-bankrupt.

4. Results

4.1. Application of the Genetic Algorithm in Bankruptcy Prediction Modeling

The sample size and the number of variables, chromosomes, and rules of each string were determined at the beginning of the modeling process. The model included 22 financial ratios as variables, five rules in each string, and an initial population of 200 chromosomes. Encoding and possible solutions of the developed algorithm were expressed as non-binary strings. Each rule includes three genes (bit): variable, variable’s sign (less or more), and variable’s amount.

In this model, the regarded field is designed as follows:

\[
\text{String} \{ \text{Var}_1, \text{Op}_1, \text{X}_1, \text{Var}_2, \text{Op}_2, \text{X}_2, \ldots \text{Var}_n, \text{Op}_n, \text{X}_n \}
\]

Rule N indicates that each rule is consisting of three elements of variable (\text{Var}), operator (\text{Op}), and amount (\text{X}) which are all randomly chosen among possible answers. In order to create the initial population, a sample of 76 companies were entered into the software as the input. The fitness of responses was then measured by the fitness function. Therefore, better fitting chromosomes had higher probability in the production of the next generation, i.e. they
produced more strings and hence omitted less fitting chromosomes. After creating the initial population, the fitness function of the total population was computed. Then, the median of all values was calculated and chromosomes with fitness function values lower than the median were regarded as unsuitable solutions and hence removed from the population. In the next stage, new solutions were created by genetic operators and previous steps were repeated. At this stage, the roulette wheel selection technique was used to select chromosomes for breeding a new generation. A random number between one and five (number of rules) was then selected as the crossover point (single point crossover). The final assimilation rate was 0.7 in this model.

Mutation was the next stage through which chromosomes were moved in the search space and the probable lost information of the population was recovered. The mutation rate was set 0.07 in this model. In the last step before the implementation of the algorithm, we determined the termination conditions as the following:

1) the most fitting chromosomes do not change after 22 times implementation of the algorithm.
2) The algorithm has been repeated 500 times; Mention must be made that in Generation, 1000 is the best model.

4.1.1. Results of the Genetic Algorithm Model:
The designed genetic algorithm model could successfully predict %92 of the bankrupt companies and %95 of non-bankrupt companies at year t-1 (one year before the base year). Its median prediction accuracy was hence %93.5 at the mentioned year (Table 3).

At year t-2 (two years before the base year), the model had an accuracy of %82 in predicting bankruptcy and %90 in predicting non-bankruptcy. The overall accuracy of the model was %86 at this year (Table 4).

Finally, three year before baseline, the model predicted bankrupt and non-bankrupt companies with accuracy of %85 and %95 respectively. The overall accuracy of the model was calculated as %90 at this year (Table 5).

<table>
<thead>
<tr>
<th>Table 2. The best fitting chromosomes after the termination of the algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>X₁ &lt; 0.082 X₂ &lt; 5.43 X₁₀ &lt; 1.146 X₁₆ &gt; 0.726 X₁₉ &lt; 0.62</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 3. Classification of the studied companies by the genetic algorithm model one year before the base year (t-1)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type of company</td>
</tr>
<tr>
<td>-----------------</td>
</tr>
<tr>
<td>Bankrupt</td>
</tr>
<tr>
<td>Non-bankrupt</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 4. Classification of the studied companies by the genetic algorithm model two years before the base year (t-2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Type of company</td>
</tr>
<tr>
<td>-----------------</td>
</tr>
<tr>
<td>Bankrupt</td>
</tr>
<tr>
<td>Non-bankrupt</td>
</tr>
</tbody>
</table>
4.2. Implementation of the Imperialist Competitive Algorithm

Similar to the genetic algorithm model, this model was also implemented using MATLAB software. At the beginning of the modeling, the initial population, number of empires, assimilation coefficient ($\beta$) and deviation angle ($\theta$), revolution rate, and the number of occurrences of evolution were determined.

To start the algorithm, 500 initial countries (all colonies) were created. Ten countries were then selected as imperialists and the remaining countries constituted the colonies. As mentioned earlier, empires with greater numbers of colonies have higher power and larger territory. Revolution rate equals 0.2, Deviation angle and revolution rate were set 45° and 0.01, respectively. The coefficient of the effect of colonies power to total empire power equals 0.02 in imperialism competitive algorithm. Algorithm termination consists of a limited number of generations, latency and change in objective function to two decimal places. The stop condition was considered 500 repetitions of the algorithm since this number of repetitions would leave only one empire and terminate the imperialistic competition.

It should be noticed that the number of countries, initial imperialists, revolution rate and time period in imperialist competitive algorithm are determined through trial and error method.

4.2.1. Results of the Imperialist Competitive Algorithm Model:

At year t-1, the designed imperialist competitive algorithm model predicted bankruptcy and non-bankruptcy with an accuracy of %98 and %95 respectively. The median prediction accuracy of the model was %96.5 at this point (Table 6).

The prediction accuracy of the model at year t-2 was %95 for both bankrupt and non-bankrupt companies. The overall accuracy of the model was hence %95 as well (Table 7).

Finally, at year t-3, the imperialist competitive algorithm model could successfully predict bankruptcy and non-bankruptcy in %98 and %95 of the cases, respectively. The overall accuracy of the model was %96.5 at this year (Table 8).

<table>
<thead>
<tr>
<th>Type of company</th>
<th>Total (n)</th>
<th>Bankrupt (n)</th>
<th>Non-bankrupt (n)</th>
<th>Bankrupt (%)</th>
<th>Non-bankrupt (%)</th>
<th>Total (%)</th>
<th>Overall accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bankrupt</td>
<td>38</td>
<td>32</td>
<td>6</td>
<td>85</td>
<td>15</td>
<td>100</td>
<td>90</td>
</tr>
<tr>
<td>Non-bankrupt</td>
<td>38</td>
<td>2</td>
<td>36</td>
<td>5</td>
<td>95</td>
<td>100</td>
<td></td>
</tr>
</tbody>
</table>

Table 6. Classification of the studied companies by the imperialist competitive algorithm model one year before the base year (t-1)

<table>
<thead>
<tr>
<th>Type of company</th>
<th>Total (n)</th>
<th>Bankrupt (n)</th>
<th>Non-bankrupt (n)</th>
<th>Bankrupt (%)</th>
<th>Non-bankrupt (%)</th>
<th>Total (%)</th>
<th>Overall accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bankrupt</td>
<td>38</td>
<td>37</td>
<td>1</td>
<td>98</td>
<td>2</td>
<td>100</td>
<td>96.5</td>
</tr>
<tr>
<td>Non-bankrupt</td>
<td>38</td>
<td>36</td>
<td>2</td>
<td>5</td>
<td>95</td>
<td>100</td>
<td></td>
</tr>
</tbody>
</table>

Table 7. Classification of the studied companies by the imperialist competitive algorithm model two year before the base year (t-2)

<table>
<thead>
<tr>
<th>Type of company</th>
<th>Total (n)</th>
<th>Bankrupt (n)</th>
<th>Non-bankrupt (n)</th>
<th>Bankrupt (%)</th>
<th>Non-bankrupt (%)</th>
<th>Total (%)</th>
<th>Overall accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bankrupt</td>
<td>38</td>
<td>36</td>
<td>2</td>
<td>95</td>
<td>5</td>
<td>100</td>
<td>95</td>
</tr>
<tr>
<td>Non-bankrupt</td>
<td>38</td>
<td>2</td>
<td>36</td>
<td>5</td>
<td>95</td>
<td>100</td>
<td></td>
</tr>
</tbody>
</table>
Table 8. Classification of the studied companies by the imperialist competitive algorithm model three year before the base year (t-3)

<table>
<thead>
<tr>
<th>Type of company</th>
<th>Total (n)</th>
<th>Bankrupt (n)</th>
<th>Non-bankrupt (n)</th>
<th>Bankrupt (%)</th>
<th>Non-bankrupt (%)</th>
<th>Total (%)</th>
<th>Overall accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bankrupt</td>
<td>38</td>
<td>37</td>
<td>1</td>
<td>98</td>
<td>2</td>
<td>100</td>
<td>96.5</td>
</tr>
<tr>
<td>Non-bankrupt</td>
<td>38</td>
<td>2</td>
<td>36</td>
<td>5</td>
<td>95</td>
<td>100</td>
<td></td>
</tr>
</tbody>
</table>

Considering the results of the designed model in three years before bankruptcy, first error is less than second error, so that the model classifies bankrupt firms more accurately than healthy firms. Low amount of the first error in proportion to the second error is necessary.

4.3. Testing the Hypotheses

The first group of hypotheses (regarding the appropriateness of the imperialist competitive algorithm and genetic algorithm models) was redefined as follows:

1. The first hypothesis: The imperialist competitive algorithm models can predict financial distress of companies registered in Tehran Stock Exchange with accuracy of more than 80%. The mean accuracy of the designed model had a 16 percent difference with the assumed value (96 vs. 80%). According to Student’s t-test, this difference was statistically significant (P=0.002). Therefore, it can be said with 99.8 certainty that the imperialist competitive algorithm is an appropriate method to predict bankruptcy.

2. The second hypothesis: The genetic algorithm models can predict financial distress of companies registered in Tehran Stock Exchange with accuracy of more than 80%. Student’s t-test suggested a significant difference between the model’s accuracy (89.84) and the assumed level (P=0.07). Thus, there is 93 certainty about the appropriateness of the genetic algorithm in bankruptcy prediction.

The second group of hypotheses involved the comparison between the two models. The mean accuracy of the imperialist competitive algorithm model (96) was 6.16 higher than that of the genetic algorithm model (89.84) (P=0.01). Hence, the imperialist competitive algorithm can predict bankruptcy with significantly higher accuracy compared to the genetic algorithm.

5. Discussion and Conclusions

Corporate bankruptcy prediction is an attractive and important issue in the field of financial research. Considering the effects of this phenomenon on micro- and macro-levels of the society, a variety of tools and models have been presented to predict bankruptcy. This study compared the imperialist competitive algorithm and genetic algorithm models and found the first to have significantly higher accuracy than the latter (96.5, 95 and 96.5 at one, two, and three years before bankruptcy vs. 93.5, 86 and 90 at the same intervals). Considering the high predictive power of the studied models, they can be used by managers to predict bankruptcy and prevent its high costs by adopting appropriate measures, by investors and financiers to make profitable financial decisions and to invest in profitable financial services, and also by auditors to comment about the ongoing activities of corporates. Regarding the type of independent variable in this study, distinguishing bankrupt firms from healthy ones is of great importance. In other words, low amount of the first error should be put higher priority. Nevertheless, none of the mentioned models can declared a company as bankrupt. Such predictions may just be warnings about a future bankruptcy (since one model might predict a company to be bankrupt while another predicts in non-bankruptcy in the future). Overall, the results of the current research can be beneficial in preventing financial distress and bankruptcy and their consequences, but after the prediction, also must be discussed tracing the root causes of problem.

References


Not’s

1 If the occurred loss destroys at least half of the company’s capital, the board of directors will be obliged to hold an extraordinary general meeting of shareholders to make a verdict about the liquidation or survival of the company. If the company is decided to survive, the company’s capital has to be reduced to the remaining capital at the same session and according to the article 6 of the Iranian commercial law.

2 If a model incorrectly considers a healthy firm as bankrupt.

3 If a model incorrectly considers a bankrupt firm as healthy.